

VECTORS & TRIG

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$a^2 + b^2 = c^2$$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$c^2 = a^2 + b^2 - 2ab \cos C$$

MOTION

$$\bar{v} = \frac{d}{t}$$

$$\bar{v} = \frac{v_f + v_i}{2}$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$v_f = v_i + a t$$

$$v_f^2 = v_i^2 + 2 a d$$

FORCES

$$F_{\text{net}} = m a$$

$$F_w = m g$$

$$F_N = F_w \cos \theta$$

$$F_{\parallel} = F_w \sin \theta$$

$$F_f = \mu F_N$$

$$F_c = m a_c = \frac{m v^2}{r}$$

PROJECTILES

$$v_x = v \cos \theta$$

$$v_y = v \sin \theta$$

$$t_{\text{total}} = \frac{2 v_y}{g}$$

$$d_x = v_x t$$

$$R = \frac{v^2 \sin 2\theta}{g}$$

MOMENTUM

$$p = m v$$

$$J = F t$$

$$J = F t = \Delta p = m v_f - m v_i$$

$$\Sigma p_{\text{before}} = \Sigma p_{\text{after}}$$

CIRCULAR AND

ROTATIONAL MOTION

$$v = \frac{2\pi r}{T} = r \omega$$

$$a_c = \frac{v^2}{r} = r \omega^2$$

$$a_t = r \alpha$$

$$F_c = m a_c = \frac{m v^2}{r}$$

$$\tan \theta = \frac{v^2}{r g} \text{ (banks)}$$

$$v_{\text{critical}} = \sqrt{g r}$$

$$\bar{\omega} = \frac{\theta}{t}$$

$$\bar{\omega} = \frac{\omega_i + \omega_f}{2}$$

$$\omega_f = \omega_i + \alpha t$$

$$\omega_f^2 = \omega_i^2 + 2 \alpha \theta$$

$$\theta = \omega_i t + \frac{1}{2} \alpha t^2$$

$$\tau = F_{\perp} r = m r^2 \alpha = I \alpha$$

$$W = \tau \theta$$

$$P = \frac{W}{t} = \frac{\tau \theta}{t} = \tau \bar{\omega}$$

$$L = I \omega$$

$$\sum L_{\text{before}} = \sum L_{\text{after}}$$

$$\Sigma \tau_{\text{clockwise}} = \Sigma \tau_{\text{counterclockwise}}$$

$$KE_{\text{rotate}} = \frac{1}{2} I \omega^2$$

$$KE_{\text{roll}} = \frac{1}{2} I \omega^2 + \frac{1}{2} m v^2$$

ENERGY

$$KE = \frac{1}{2} m v^2$$

$$PE = m g h$$

$$W = F d$$

$$P = \frac{W}{t} = F \bar{v}$$

$$AMA = \frac{F_{\text{out}}}{F_{\text{in}}}$$

$$IMA = \frac{d_{\text{in}}}{d_{\text{out}}}$$

$$Eff = \frac{AMA}{IMA} = \frac{W_{\text{out}}}{W_{\text{in}}} = \frac{P_{\text{out}}}{P_{\text{in}}}$$

MACHINE IMA'S

$$\text{incline} = \frac{\text{length}}{\text{height}}$$

$$\text{lever} = \frac{\text{effort arm length}}{\text{load arm length}}$$

$$\text{wheel \& axle} = \frac{r_{\text{wheel}}}{r_{\text{axle}}} = \frac{D_{\text{wheel}}}{D_{\text{axle}}}$$

$$\text{pulley} = \# \text{ support ropes}$$

$$\text{screw} = \frac{2\pi r}{\text{pitch}}$$

SPRINGS & SHM

$$F = k x$$

$$W_{\text{spring}} = PE_e = \frac{1}{2} k x^2$$

$$T = \frac{1}{f}$$

$$T_{\text{spring}} = 2\pi \sqrt{\frac{m}{k}}$$

$$T_{\text{pendulum}} = 2\pi \sqrt{\frac{L}{g}}$$

$$\omega = \frac{2\pi}{T} = 2\pi f$$

$$v_x = -A \omega \sin \omega t$$

$$v_{\text{max}} = A \omega$$

$$a_x = -A \omega^2 \cos \omega t$$

$$a_{\text{max}} = A \omega^2$$

$$\omega = \sqrt{\frac{k}{m}}$$

GRAVITATION

$$F = \frac{G m_1 m_2}{d^2}$$

$$g = \frac{G M}{r^2}$$

$$v_{\text{escape}} = \sqrt{\frac{2 G M}{r}} = \sqrt{2 g r}$$

$$v_{\text{orbit}} = \sqrt{\frac{G M}{r}}$$

$$G = 6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}$$

$$T^2 = K r^3$$

$$K = 2.97 \times 10^{-19} \frac{\text{s}^2}{\text{m}^3}$$

WAVES & SOUND

$$v = \lambda f$$

$$v_{\text{sound}} = 330 \frac{m}{s} + .6 \frac{m/s}{^\circ C}$$

$$v = \sqrt{\frac{F}{m/L}}$$

$$I = \frac{P}{A} = \frac{P}{4\pi r^2}$$

$$\beta = (10\text{dB}) \log \frac{I}{I_0}$$

$$\Delta\beta = (10\text{dB}) \log \frac{I_2}{I_1}$$

$$f_l = f_s \frac{v + v_l}{v - v_s}$$

$$f_n = \frac{nv}{2L} (\text{string, open tube}) n = 1, 2, 3, \dots$$

$$f_n = \frac{nv}{4L} (\text{tube open one end}) n = 1, 3, 5, \dots$$

$$\sin \theta = \frac{\lambda}{D} (\text{square opening})$$

$$\sin \theta = 1.22 \frac{\lambda}{D} (\text{round opening})$$

PROPERTIES OF FLUIDS

$$\rho = \frac{m}{V}$$

$$P = \frac{F}{A}$$

$$P = \rho gh$$

$$P_2 = P_1 + \rho gh (\text{absolute})$$

$$P_2 - P_1 = \rho gh (\text{gauge})$$

$$\frac{F_1}{A_1} = \frac{F_2}{A_2}$$

$$F_B = W_{\text{fluid}} = mg = \rho Vg$$

$$\rho_1 A_1 v_1 = \rho_2 A_2 v_2$$

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho gh_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho gh_2$$

THERMODYNAMICS

$$\Delta U = Q - W$$

$$\Delta U = \frac{3}{2} nR\Delta T$$

$$W = P\Delta V = nR\Delta T (\text{isobaric})$$

$$W = nRT \ln \frac{V_2}{V_1} (\text{isothermal})$$

$$W = -\frac{3}{2} nR\Delta T (\text{adiabatic})$$

$$P_1 V_1^\gamma = P_2 V_2^\gamma (\text{adiabatic})$$

$$Q_V = C_V n\Delta T (C_V = \frac{3}{2} R)$$

$$Q_P = C_P n\Delta T (C_P = \frac{5}{2} R)$$

$$R = 8.31 \frac{J}{\text{mol} \cdot K}$$

$$Eff = \frac{W}{Q_h} = \frac{Q_h - Q_c}{Q_h} = 1 - \frac{Q_c}{Q_h} (\text{real engine})$$

$$Eff = 1 - \frac{T_c}{T_h} (\text{carnot engine})$$

$$\frac{Q_c}{Q_h} = \frac{T_c}{T_h} (\text{carnot engine})$$

$$\Delta S = \frac{Q}{T}$$

$$COP = \frac{Q_c}{W} (\text{air conditioner})$$

$$COP = \frac{Q_h}{W} (\text{heat pump})$$

PROPERTIES OF GASES

$$PV = nRT = NkT$$

$$R = 8.31 \frac{J}{\text{mol} \cdot K}$$

$$k = 1.38 \times 10^{-23} \frac{J}{K}$$

$$P_1 V_1 = P_2 V_2$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\overline{KE} = \frac{1}{2} m v_{\text{rms}}^2 = \frac{3}{2} kT$$

PROPERTIES OF SOLIDS

$$\rho = \frac{m}{V}$$

$$P = \frac{F}{A}$$

$$Y = \frac{FL_0}{A\Delta L}$$

$$S = \frac{FL_0}{A\Delta X}$$

$$\Delta P = -B \frac{\Delta V}{V_0}$$

$$Q = mc\Delta T (\text{same phase})$$

$$Q = mL_f (\text{fusion})$$

$$Q = mL_v (\text{vaporization})$$

$$\Delta L = \alpha L_0 \Delta T$$

$$\Delta V = \beta V_0 \Delta T$$

$$Q = \frac{kA\Delta T t}{L}$$

$$Q = \frac{A\Delta T t}{R}$$

$$Q = e\sigma AT^4 t$$

$$\sigma = 5.67 \times 10^{-8} \frac{J}{s \cdot m^2 \cdot K^4}$$

CONSTANTS

$$g = 9.80 \frac{m}{s^2}$$

$$M_{\text{earth}} = 5.98 \times 10^{24} \text{kg}$$

$$r_{\text{earth}} = 6.38 \times 10^6 \text{m}$$

$$c = 3.00 \times 10^8 \frac{m}{s}$$

$$m_{p^+} = 1.67 \times 10^{-27} \text{kg}$$

$$m_{e^-} = 9.11 \times 10^{-31} \text{kg}$$

$$q_{p^+} = 1.602 \times 10^{-19} \text{C}$$

$$q_{e^-} = -1.602 \times 10^{-19} \text{C}$$